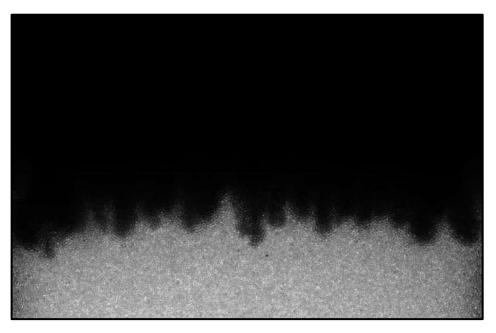
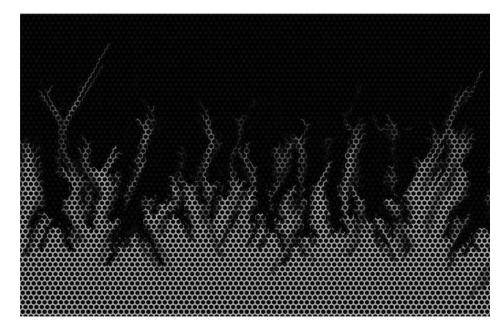
Experimental and numerical investigation on convective mixing in porous media flows



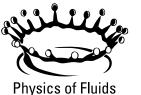


M. De Paoli^{1,2}, C. Howland¹, R. Verzicco^{1,3,4} & D. Lohse^{1,5}



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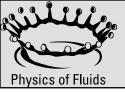
⁵Max Plank Institute for Dynamics and Self-Organization, Göttingen (Germany)



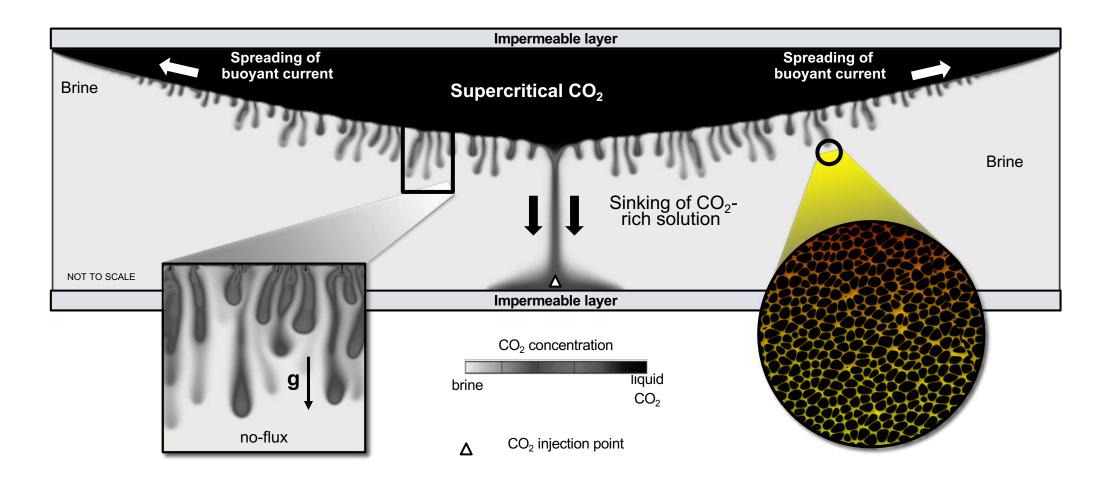
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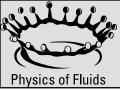


Convection in complex multiphase and multiscale systems

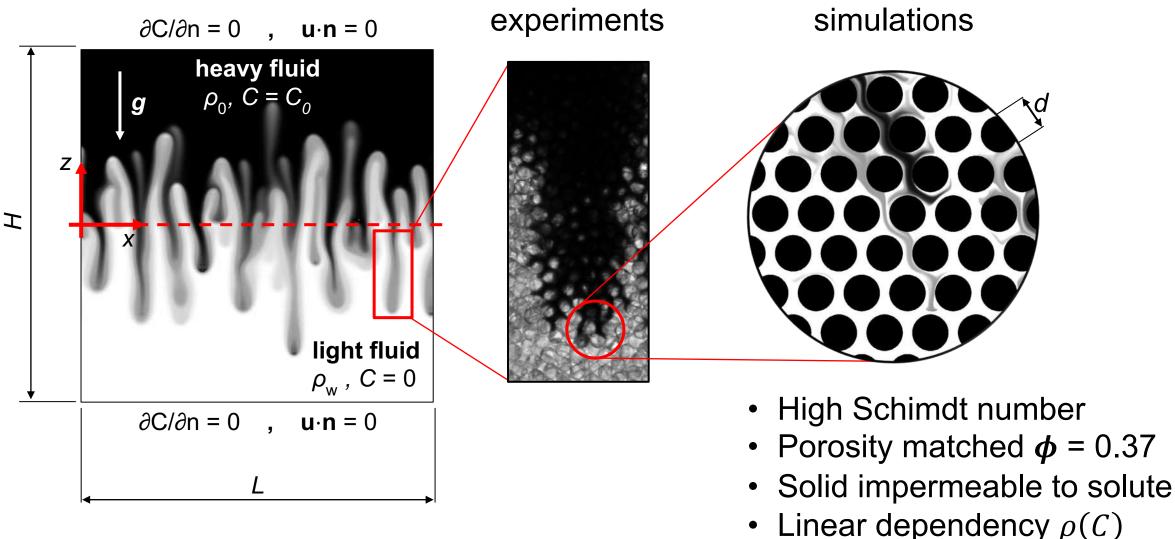


De Paoli, Phys. Fluids (2021)

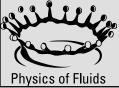




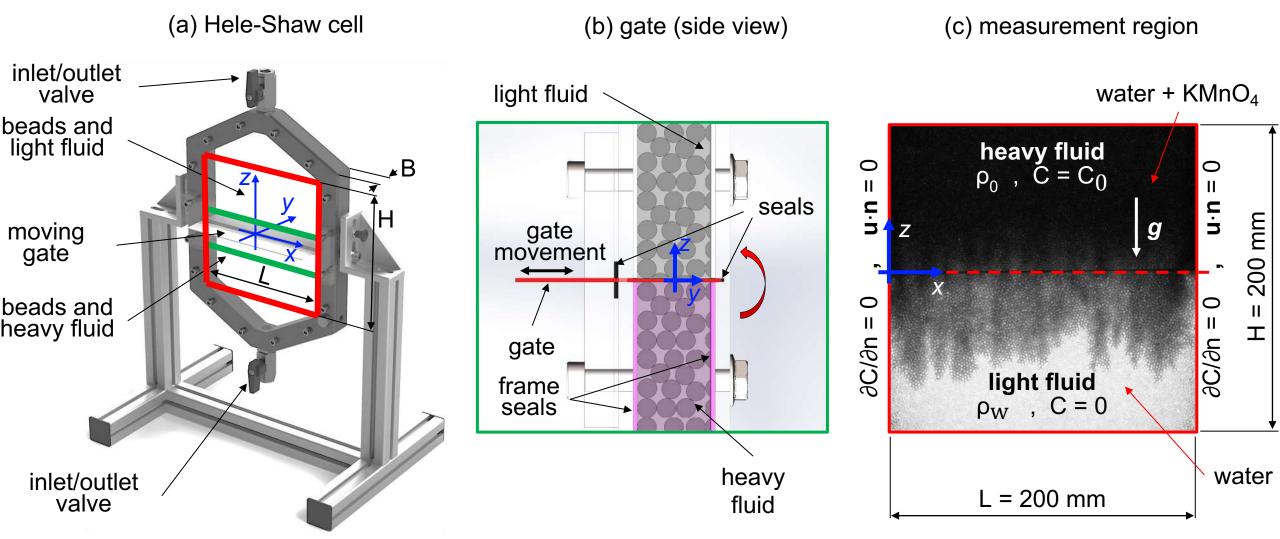
Flow configuration





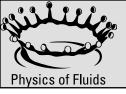


Experimental setup

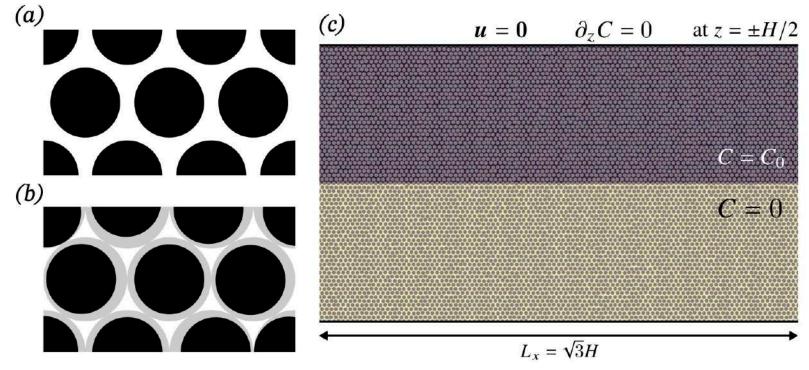


Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente





Numerical method



$$\partial_t \boldsymbol{u} + (\boldsymbol{u} \cdot \boldsymbol{\nabla})\boldsymbol{u} = -\rho_0^{-1}\boldsymbol{\nabla}p + \boldsymbol{v}\boldsymbol{\nabla}^2\boldsymbol{u} - g\beta C\hat{\boldsymbol{z}},$$

$$\partial_t C + (\boldsymbol{u} \cdot \boldsymbol{\nabla})C = D\boldsymbol{\nabla}^2 C,$$

$$\rho = \rho_0 \bigg[1 + \frac{\Delta\rho}{\rho_0 C_0} (C - C_0) \bigg]$$

Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente Advanced finite difference (AFiD, open source) + Immersed Boundaries Method

Resolution:

- velocity: ≥ 32 points per diameter
- concen.: ≥ 128
 points per diameter



withing.
Physics of Fluids

experiments										
Name	H/d	ϕ	Sc	Ra	<i>Ra</i> _d	Ra^*	Pe	Re		
E1	200	0.37	558	4.535×10 ¹⁰	5.669×10^{3}	2.173×10^{3}	0.289	0.0005		
E2	200	0.37	558	9.099×10^{10}	1.137×10^4	4.359×10^{3}	0.580	0.0010		
E3	200	0.37	558	1.824×10^{11}	2.280×10^4	8.737×10^{3}	1.163	0.0021		
E4	200	0.37	558	3.637×10^{11}	4.546×10^{4}	1.742×10^{4}	2.320	0.0042		
E5	114	0.37	558	4.667×10 ¹⁰	3.126×10 ⁴	6.846×10^3	1.595	0.0029		
E6	114	0.37	558	9.099×10 ¹⁰	6.096×10^4	1.335×10^{4}	3.110	0.0056		
E7	114	0.37	558	1.820×10^{11}	1.219×10^{5}	2.671×10^4	6.222	0.0112		
E8	114	0.37	558	3.626×10^{11}	2.429×10^5	5.320×10^4	12.395	0.0222		
E9	67	0.35	558	4.490×10 ¹⁰	1.515×10^{5}	1.627×10^4	5.795	0.0104		
E10	67	0.35	558	9.495×10^{10}	3.204×10^{5}	3.441×10^4	12.256	0.0220		
E11	67	0.35	558	1.834×10^{11}	6.189×10^5	6.646×10^4	23.672	0.0425		
E12	67	0.35	558	3.670×10^{11}	1.239×10^{6}	1.330×10^{5}	47.370	0.0850		
E13	50	0.37	558	4.506×10 ¹⁰	3.605×10 ⁵	3.454×10^4	18.393	0.0330		
E14	50	0.37	558	9.101×10^{10}	7.281×10^{5}	6.976×10^4	37.150	0.0666		
E15	50	0.37	558	1.824×10^{11}	1.460×10^{6}	1.398×10^{5}	74.474	0.1336		
E16	50	0.37	558	3.622×10 ¹¹	2.898×10^{6}	2.777×10^5	147.861	0.2652		

flow scales and parameters

 $k = \frac{d^2}{36k_C} \frac{\phi^3}{(1-\phi)^2}$

$$U = \frac{g\Delta\rho k}{\mu}$$

$$\ell = \frac{\phi D}{U}$$

$$Sc = \frac{\mu}{\rho_0 I}$$

$$\frac{\mu}{\rho_0 D}$$
 Ra

$$Da = k/H^2$$

$$Ra Da$$

$$Ra = \frac{g\Delta\rho H^3}{\mu D}$$
$$Re = \frac{Ra^* Da^{1/2}}{Sc}$$

dimensionless parameters

$$Ra_d = -\mu$$

ח

$$Pe = Ra^* Da^{1/2}$$

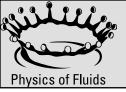
 $g\Delta\rho d^2$



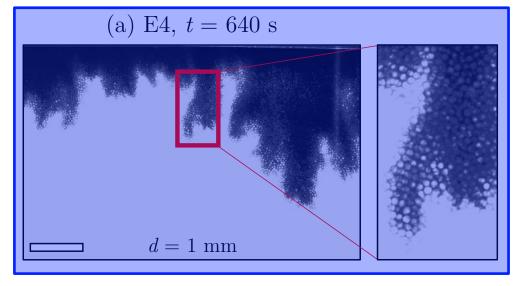
Name	H/d	ϕ	Sc	Ra	Ra _d	Ra*	Pe	Re
S 1	17	0.37	100	5.268×10 ⁸	1.000×10^5	3.334×10 ³	5.102	0.0510
S2	17	0.37	100	1.666×10 ⁹	3.162×10^{5}	1.054×10^4	16.135	0.1614
S 3	17	0.37	100	5.268×10^{9}	1.000×10^{6}	3.334×10^{4}	51.024	0.5102
S4	35	0.37	100	4.214×10 ⁹	1.000×10^{5}	6.669×10 ³	5.102	0.0510
S5	35	0.37	100	1.333×10^{10}	3.162×10^5	2.109×10^4	16.135	0.1614
S 6	35	0.37	100	4.214×10^{10}	1.000×10^{6}	6.669×10^4	51.024	0.5102
S 7	52	0.37	100	1.422×10^{10}	1.000×10^5	1.000×10^4	5.102	0.0510
S 8	52	0.37	100	4.498×10^{10}	3.162×10^5	3.163×10^4	16.135	0.1614
S 9	52	0.37	100	1.422×10^{11}	1.000×10^{6}	1.000×10^5	51.024	0.5102
S 10	70	0.37	100	3.372×10 ¹⁰	1.000×10^5	1.334×10 ⁴	5.102	0.0510
S11	70	0.37	100	1.066×10^{11}	3.162×10^5	4.218×10^{4}	16.135	0.1614
S12	70	0.37	100	3.372×10^{11}	1.000×10^{6}	1.334×10^{5}	51.024	0.5102

simulations

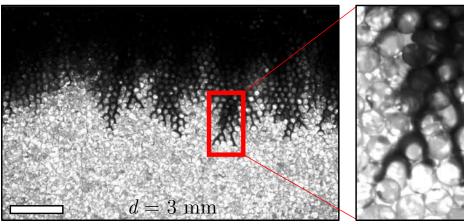
6



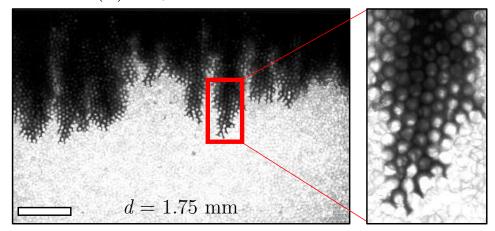
Influence of $d (\Delta \rho = 7 \text{ kg/m}^3)$



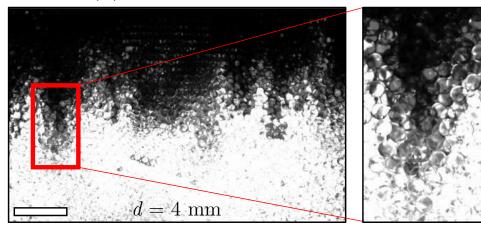
(c) E12, t = 121 s



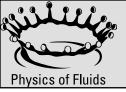
Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente (b) E8, t = 206 s



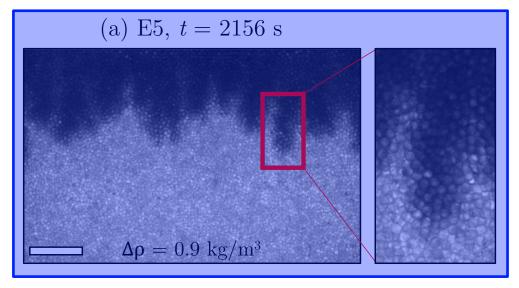
(d) E16, t = 59 s



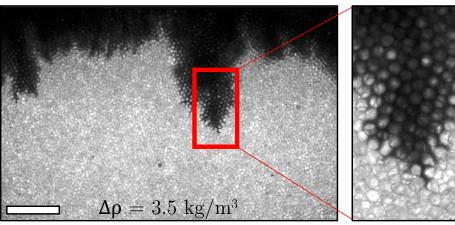




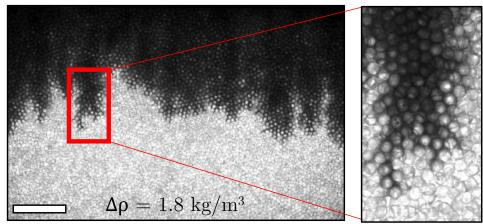
Influence of $\Delta \rho$ (*d* = 1.75 mm)



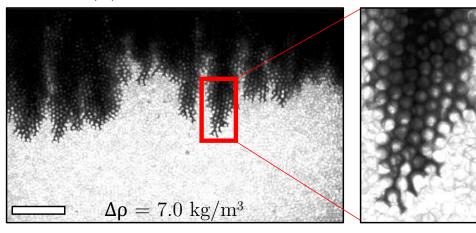
(c) E7, t = 368 s



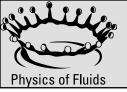
Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente (b) E6, t = 748 s



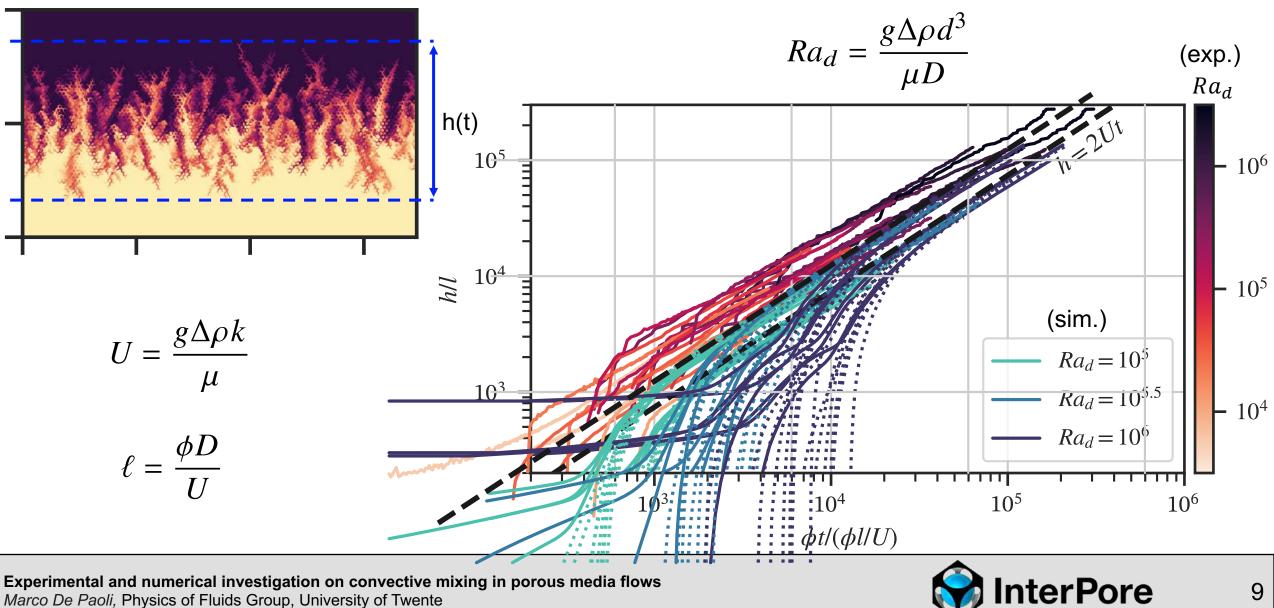
(d) E8, t = 206 s



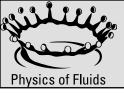




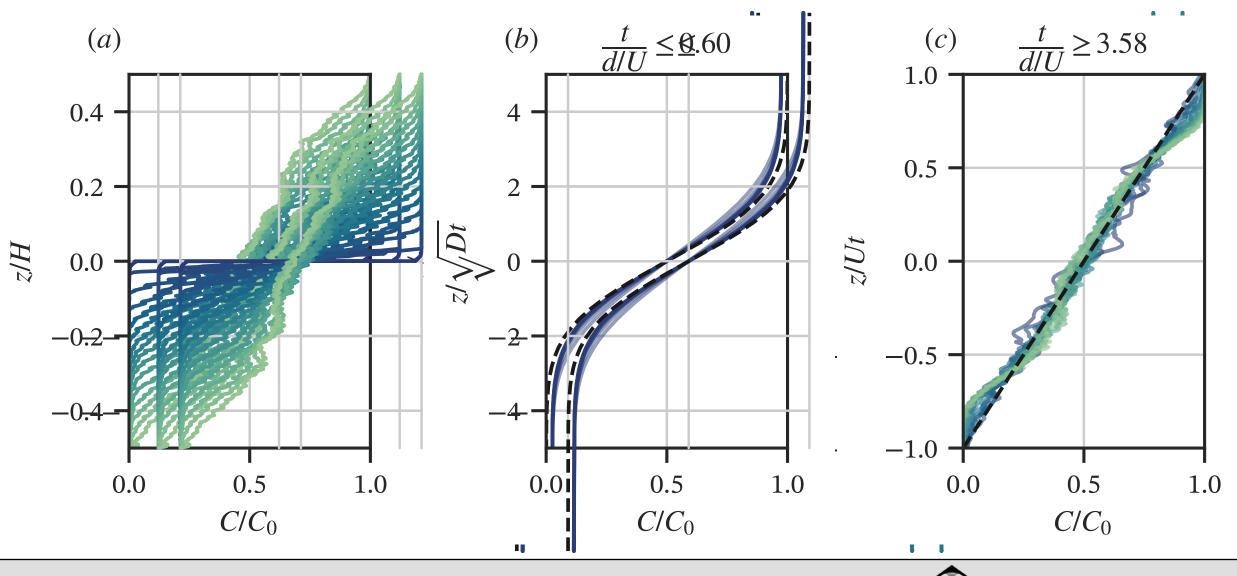
Mixing length



Marco De Paoli, Physics of Fluids Group, University of Twente



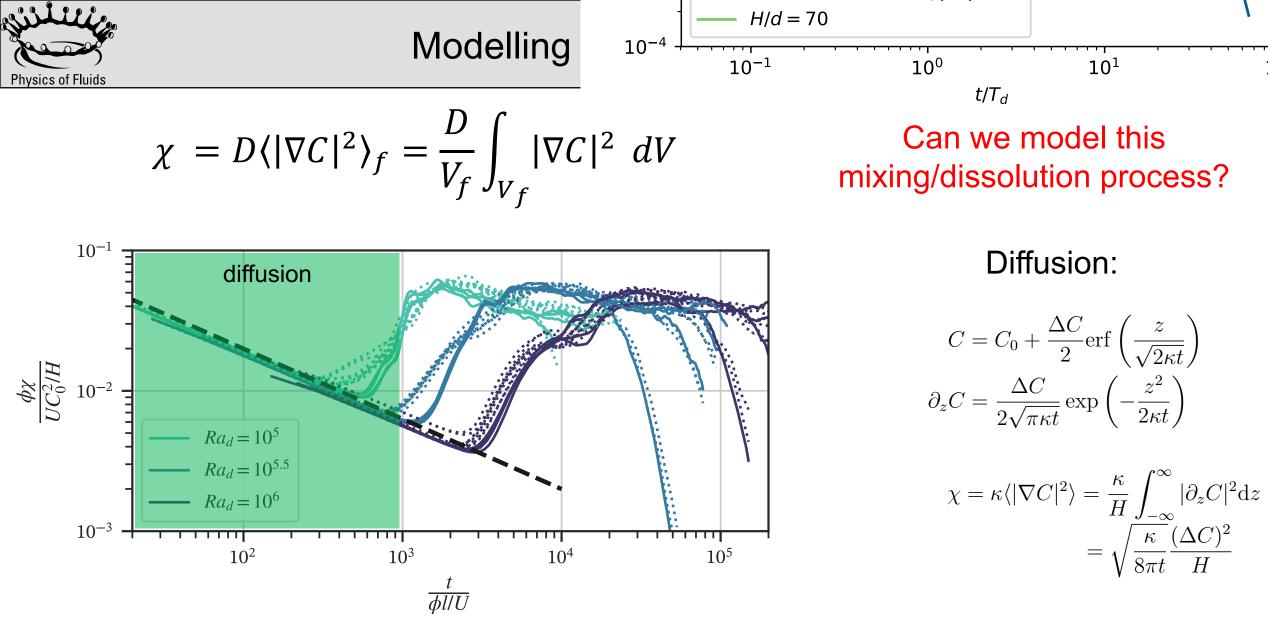
Concentration profiles



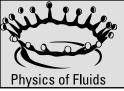
Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente



InterPore

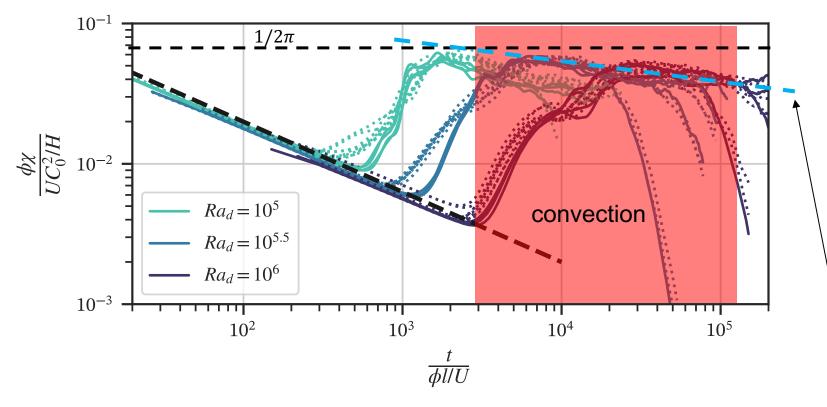






Modelling scalar dissipation

$$\chi = D\langle |\nabla C|^2 \rangle_f = \frac{D}{V_f} \int_{V_f} |\nabla C|^2 \, dV$$



Convection $\chi = \kappa \langle |\nabla C|^2 \rangle = \kappa \frac{L_m}{H} \langle |\nabla C|^2 \rangle_{ML},$ $|\nabla C| \approx \frac{\Delta C}{2\sqrt{\pi\kappa t}}.$

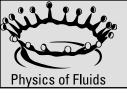
 $L_m \approx 2Ut,$

$$\chi \approx \kappa \frac{2Ut}{H} \frac{(\Delta C)^2}{4\pi\kappa t} = \frac{1}{2\pi} \frac{U_d (\Delta C)^2}{H}.$$

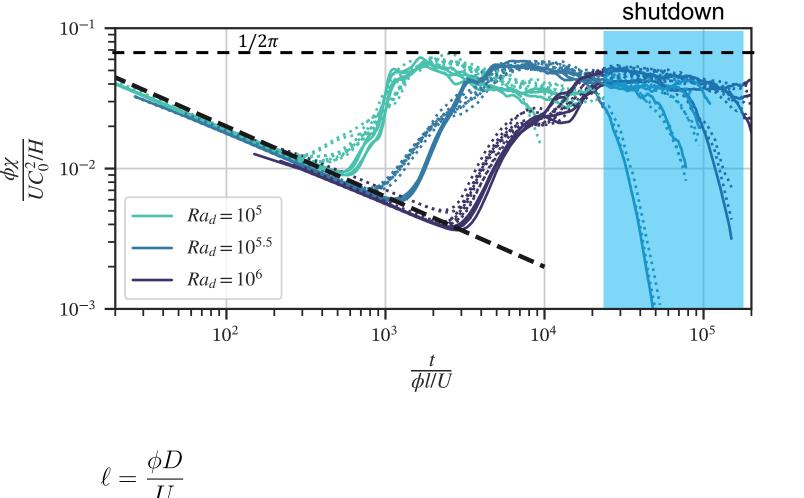
 $1/2\pi$ is the maximum value of dissipation. Practically, χ decreases with time



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Modelling scalar dissipation

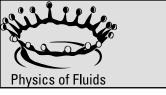


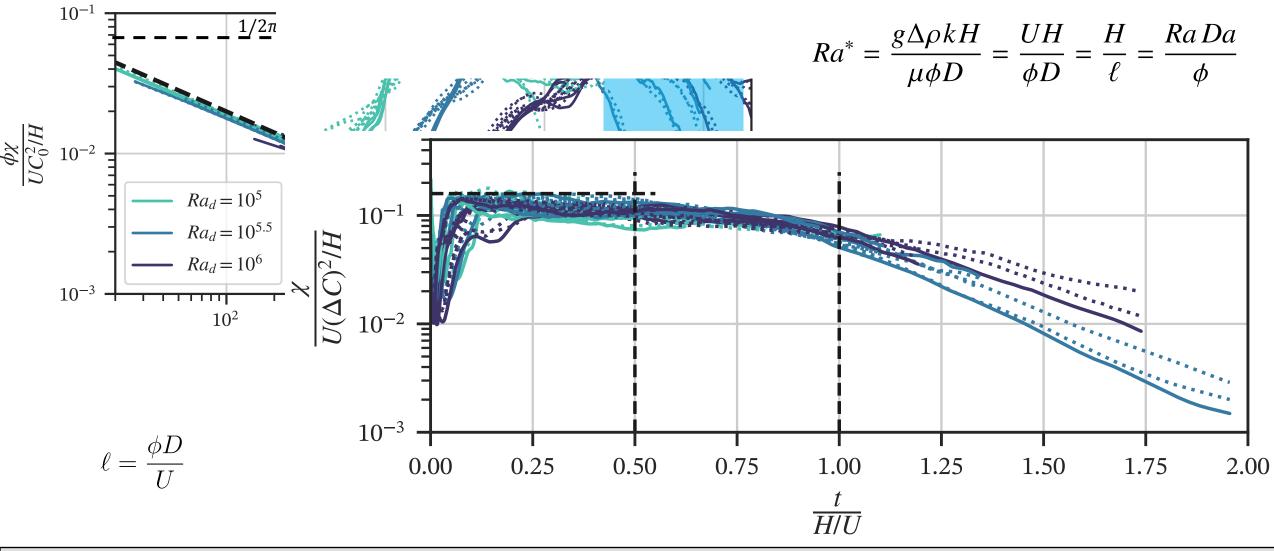
 $Ra^* = \frac{g\Delta\rho kH}{\mu\phi D} = \frac{UH}{\phi D} = \frac{H}{\ell} = \frac{RaDa}{\phi}$

U

Experimental and numerical investigation on convective mixing in porous media flows *Marco De Paoli,* Physics of Fluids Group, University of Twente







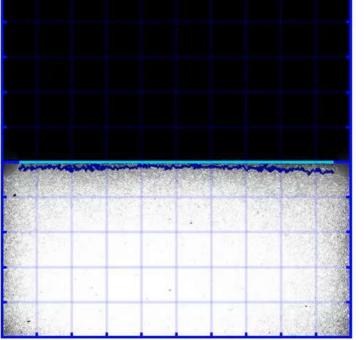


Conclusions

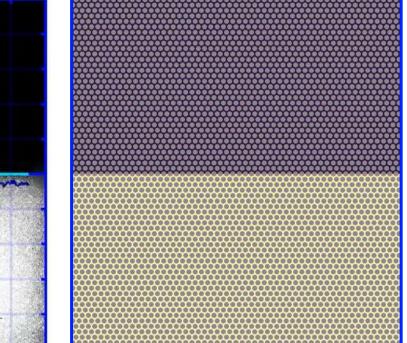
- Simulations and experiments are used as complementary tools to investigate convection in porous media
- Multiple length scales are relevant at different phases of the process

Physics of Fluids

- Mixing length predicted experimentally exhibits a self-similar behaviour that agrees well with theoretical prediction for convective flows in porous media
- Mixing measured numerically via mean scalar dissipation has a self-similar behaviour.
- We explain theoretically the scaling laws observed
- We plan to expand the parameters space investigated and performed simulations in three-dimensional domains



This research was funded in part by the Austrian Science Fund (FWF) [Grant J-4612]



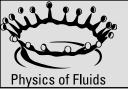
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Der Wissenschaftsfonds.

Thank you for your attention! Questions?





High-resolution images, movies and slides are available upon request to m.depaoli@utwente.nl

